

# The Aster Package Tutorial

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## 1 Preliminaries

### 1.1 Warning

A redesign of the calling sequence of the functions

```
aster  
predict.aster  
predict.aster.formula
```

is underway. Some of the details of what follows is likely to change in a future version (real soon now).

### 1.2 Library and Data

```
> library(aster)  
> data(echinacea)
```

That's our package and the dataset for our examples.

### 1.3 Digression on Data Entry

The simplest way to enter your own data into R is to construct a plain text file that is a white-space-separated matrix of numbers with column headings. (Note this means not touched by Microsoft Word or any so-called word processors that are incapable of not garbaging up plain text with a lot of unwanted formatting junk: if on Microsoft Windows, use Microsoft Notepad.)

An example is the file "`echinacea.txt`" found in the `data` directory of the package installation.

This file could read into R as follows

```
echinacea <- read.table("echinacea.txt", header = TRUE)
```

In fact that's what R did when loading the library.

If you have been so foolish as to give your data to Microsoft Excel, you can ask it to give it back by writing out in CSV (Microsoft comma separated values format), and it may give you back something usable (or it may not: dates are especially problematic, for some reason). If the output is called `echinacea.csv` then

```
echinacea <- read.csv("echinacea.csv")
```

will read it into R.

## 1.4 Digression on Data Frames

In either case the R object `echinacea` created by the `data` statement or a `read.table` or `read.csv` command is what R calls a *data frame*. It prints like a matrix but is really a list of vectors of the same length. The command

```
> names(echinacea)
```

```
[1] "hdct02" "hdct03" "hdct04" "site"   "ewloc"  "nsloc"
[7] "ld02"   "f102"   "ld03"   "f103"   "ld04"   "f104"
```

shows the names of these (vector) variables. The names are the column headings from the input file. Any variables having character values have been coerced to what R calls *factors*. To see what kind of variable each is we can do

```
> sapply(echinacea, class)
```

```
      hdct02      hdct03      hdct04      site      ewloc      nsloc
"integer" "integer" "integer"  "factor" "integer" "integer"
      ld02      f102      ld03      f103      ld04      f104
"integer" "integer" "integer" "integer" "integer" "integer"
```

In the `echinacea` data set, the variables with numbers in the names are the columns of the response matrix of the aster model.

- The variables `ld0x` (where  $x$  is a digit) are the survival indicator variables for year  $200x$  (one for alive, zero for dead).
- The variables `f10x` are the flowering indicator variables (one for any flowers, zero for none).

- The variables `hdct0x` are the inflorescence (flower head) count variables (number of flower heads).

The variables without numbers are other predictors.

- The variables `ewloc` and `nsloc` are spatial, east-west and north-south location, respectively.
- The variable `site` is the site of origin of the plant, so plants with different values of `site` may be more genetically diverse than those with the same values of `site`.

The point of recording the data about flowers in two variables `f10x` and `hdct0x` for any given  $x$  when the single variable `hdct0x` contains the same information (because `f10x` = 0 if and only if `hdct0x` = 0) is because there is no good, simple statistical model for `hdct0x` by itself.

As we shall see, it makes sense to model the conditional distribution of `f10x` given `ld0x` = 1 as Bernoulli and it makes sense to model the conditional distribution of `hdct0x` given `f10x` = 1 as Poisson conditioned on being nonzero. But it would not make sense to model `hdct0x` given `ld0x` = 1 as Poisson. The case of zero flowers is special and must be modeled separately.

## 1.5 Digression on Reshape

Standard regression-like modeling requires that the “response” be a vector. The “response” (“data” would be a better name since it plays two roles:  $X_{ip(j)}$  is the sample size for  $X_{ij}$ ) is a matrix. If we are going to use any of the R apparatus for doing regression-like modeling, in particular if we are going to use the R formula mini-language that allows model specifications like `y ~ x1 + x2` then we need to make the response (the `y` in the formula) a vector.

There is an R function `reshape` that does this

```
> vars <- c("ld02", "ld03", "ld04", "f102", "f103",
+          "f104", "hdct02", "hdct03", "hdct04")
> redata <- reshape(echinacea, varying = list(vars),
+                  direction = "long", timevar = "varb", times = as.factor(vars),
+                  v.names = "resp")
> names(redata)

[1] "site" "ewloc" "nsloc" "varb" "resp" "id"
```

making a new data frame (in this case **redata**) that has new variables (all of the same length because they are in the same data frame)

**resp** which contains all of the data in the variables indicated by the string **vars** packed into a single vector, the name **resp** being given by the **v.names** argument of the **reshape** function (you could make it anything you like),

**varb** which indicates which original variable the corresponding element of **resp** came from, the name being given by the **timevar** argument of the **reshape** function, and

**id** which indicates which original individual the corresponding element of **resp** came from, the name being given by the **idvar** argument of the **reshape** function (which we didn't specify, accepting the default value "id").

**Warning** The variable **vars** must have the variables listed with parent nodes before child nodes. This doesn't make sense now, but is necessary to satisfy condition (\*) on page 5.

Let's look at an example

```
> redata[42, ]

      site ewloc nsloc varb resp id
42.1d02  SPP   -3     7 1d02   1 42
```

This says that the 42nd row of the data frame **redata** has response value 1. This is the response for the 1d02 original variable (node of the graphical model) and for individual 42 found in row 42 of the original data frame **echinacea**. The other variables **site**, **ewloc**, and **nsloc** are what they were in this row of **echinacea** (for this original individual) and are duplicated as necessary in other rows of **redata**.

## 2 Unconditional Aster Models

Now we are ready to begin discussion of Aster models. First we load the package.

```
> library(aster)
```

## 2.1 More Preliminaries

Then more details. We must define a few more variables that determine the structure of the aster model we intend to work with. The variable `resp` contains only the random data. There is also the non-random data on the root nodes of the dependence graph of the model. For reasons having to do with the way the R formula mini-language works, we usually want this in the same data frame as `resp`

```
> redata <- data.frame(redata, root = 1)
> names(redata)

[1] "site" "ewloc" "nsloc" "varb" "resp" "id" "root"
```

This adds a variable `root` to the data frame and makes all its values one (including for non-root nodes, but those values are ignored by all `aster` package functions).

We also need two vectors of the same length as the number of nodes in the graph (so they cannot go in the data frame `redata`), call that length `nnode`

```
> pred <- c(0, 1, 2, 1, 2, 3, 4, 5, 6)
> fam <- c(1, 1, 1, 1, 1, 1, 3, 3, 3)
> families()[fam]

[1] "bernoulli"      "bernoulli"      "bernoulli"
[4] "bernoulli"      "bernoulli"      "bernoulli"
[7] "non.zero.poisson" "non.zero.poisson" "non.zero.poisson"
```

`pred` specifies the predecessor structure of the graph. With the original variables indexed from 1 to `nnode`, in the order that they appear in the variable `vars` defined above and supplied as the `varying` argument to the `reshape` function, `pred[j]` gives the index of the predecessor of node `j`. In order to make it obvious that `pred` specifies an acyclic graph, we require

$$\text{all}(\text{pred} < \text{seq}(\text{along} = \text{pred})) \quad (*)$$

hold. If `pred[j] == 0` this indicates `j` indexes a root node (no predecessor).

`fam` specifies the one-parameter exponential families for the nodes: `fam[j]` gives the index of the family for node `j`, the index being for the vector of family names returned by `families()`.

**Comment** Using an index vector rather than a character vector for `fam` is definitely not the R way. But having decided to make `pred` an index vector, the same seemed natural for `fam`.

The reason for using an index vector for `pred` is so the condition (\*) makes sense. The original variables must be related to their order in the data frame `redata` in any case.

**Warning** This may change in the future, but that's the way it is for now. In fact it is very likely to change in the future and in a non-backwards-compatible way (see the warning in Sec 1.1).

## 2.2 Fitting a Model

We are finally ready to fit a model.

```
> aout1 <- aster(resp ~ varb + nsloc + ewloc + site,
+               pred, fam, varb, id, root, data = redata)
> summary(aout1, show.graph = TRUE)
```

Call:

```
aster.formula(formula = resp ~ varb + nsloc + ewloc + site, pred = pred,
              fam = fam, varvar = varb, idvar = id, root = root, data = redata)
```

Graphical Model:

variable	predecessor	family
ld02	root	bernoulli
ld03	ld02	bernoulli
ld04	ld03	bernoulli
fl02	ld02	bernoulli
fl03	ld03	bernoulli
fl04	ld04	bernoulli
hdct02	fl02	non.zero.poisson
hdct03	fl03	non.zero.poisson
hdct04	fl04	non.zero.poisson

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-1.429438	0.184006	-7.768	7.95e-15 ***
varbfl03	-0.329497	0.265611	-1.241	0.21478
varbfl04	-0.355326	0.241242	-1.473	0.14078
varbhdct02	1.715376	0.249520	6.875	6.21e-12 ***

```

varbhdct03  1.733264  0.200166  8.659 < 2e-16 ***
varbhdct04  2.246177  0.185538 12.106 < 2e-16 ***
varbld02    -0.967928  0.311876 -3.104 0.00191 **
varbld03     0.793777  0.392935  2.020 0.04337 *
varbld04     3.932665  0.330810 11.888 < 2e-16 ***
nsloc        0.013684  0.001733  7.895 2.91e-15 ***
ewloc        0.006003  0.001727  3.475 0.00051 ***
siteEriley  -0.052273  0.053504 -0.977 0.32857
siteLf       -0.046125  0.056892 -0.811 0.41751
siteNessman -0.124857  0.070894 -1.761 0.07821 .
siteNWLF     -0.061712  0.051028 -1.209 0.22652
siteSPP       0.036007  0.054506  0.661 0.50887
siteStevens -0.084581  0.054256 -1.559 0.11901

```

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

The `show.graph = TRUE` makes the table about the graph structure in the printout. You always want to look at that carefully once, since it tells you whether you have gotten it right. But (unless you change `redata`, `pred`, or `fam`) it won't change thereafter. Hence the default is to not print it.

**Interpretation.** From looking at the “signif. stars” it looks like `site` is not significant. But you're not supposed to use “signif. stars” that way. Any use of more than one “signif. stars” per model fit is *multiple testing without correction* and may be *highly misleading*. Wise users put

```
> options(show.signif.stars = FALSE)
```

in their `.Rprofile` file so they aren't even tempted to foolishness by them. The R default is to print them, so that's what `summary.aster` does too.

## 2.3 Model Comparison

The right way to compare models is with a likelihood ratio test. To do that, you must fit two models. So here's another.

```
> aout2 <- aster(resp ~ varb + nsloc + ewloc, pred,
+               fam, varb, id, root, data = redata)
```

Now we can compare them with

```
> anova(aout2, aout1)
```

### Analysis of Deviance Table

Model 1: `resp ~ varb + nsloc + ewloc`

Model 2: `resp ~ varb + nsloc + ewloc + site`

	Model	Df	Model Dev	Df	Deviance	P(> Chi )
1	11	2747.90				
2	17	2734.38	6	13.52	0.04	

So much for making inferences from a bunch of signif. stars! Not one of the signif. stars for the `site` dummy variables in the printout for `about1` was anywhere near as significant as the likelihood ratio test  $p$ -value here. See what we mean?

**Warning** (copied from the `anova.aster` help page)

The comparison between two or more models ... will only be valid if they are (1) fitted to the same dataset, (2) models are nested, (3) models are of the same type (all conditional or all unconditional), (4) have the same dependence graph and exponential families. None of this is currently checked.

You're not likely to botch (1) or (4). Just make sure you use the same data frame and the same `pred` and `fam`. If you're a little careful, you won't botch (3). We haven't done conditional models yet (see Section 4), but if careful one should not botch that (conditional and unconditional models are like apples and oranges, they shouldn't be mixed). The hard condition to always obey is (2). One must be sure that the column space of the model matrix of the big model (`about1$modmat`) contains the column space of the model matrix of the small model (`about2$modmat`), but that is much easier checked by the computer than by you.

**Comment** So perhaps the computer should check all this, despite none of the R `anova` functions doing so. It would take time, enough for one linear regression per column of the model matrix of the small model. But it would add safety. But the R/C/Unix way (a. k. a., worse is better) is to not check and let the user worry about it.

Anyway (as the warning says) `anova.aster` and `anova.asterlist` currently do not check. The user must make sure the models are nested (otherwise the comparison is theoretically rubbish).



## 2.4 Models Based on Pseudo-Covariates

In a sense the “covariate” variable `varb` is already a pseudo-covariate. It’s not a measured variable. It’s an artifice we use to overcome the limitations of the R formula mini-language insisting that the “response” be a vector, rather than a matrix with heterogenous columns (like it really is).

In this section we do more artifice. The variables of interest, that are “components of fitness” in the evolutionary jargon are the `hdct` variables. We want to look that the interaction of site with those variables. So first we have to create the relevant dummy variable.

```
> hdct <- grep("hdct", as.character(redata$varb))
> hdct <- is.element(seq(along = redata$varb), hdct)
> redata <- data.frame(redata, hdct = as.integer(hdct))
> names(redata)

[1] "site" "ewloc" "nsloc" "varb" "resp" "id" "root"
[8] "hdct"
```

This is tricky. The variable `redata$varb` is a factor, which means it is really numeric (an index vector) under the hood, even though it prints as a character string. To get the strings to work with we do `as.character(redata$varb)`. Then the first statement returns the *indices* of the elements of `varb` whose string forms contain “hdct”. The next statement converts these to TRUE or FALSE. The third statement converts these to one and zero, and makes them the variable `hdct` in the data frame `redata`. You might not think of such an R-ish way to do this, but if you want to use such a variable in modeling, you must create it somehow.

Now we can fit an interaction term.

```
> aout3 <- aster(resp ~ varb + nsloc + ewloc + site *
+   hdct, pred, fam, varb, id, root, data = redata)
> summary(aout3)
```

Call:

```
aster.formula(formula = resp ~ varb + nsloc + ewloc + site *
  hdct, pred = pred, fam = fam, varvar = varb, idvar = id,
  root = root, data = redata)
```

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-1.583649	0.216993	-7.298	2.92e-13
varbf103	-0.328716	0.264185	-1.244	0.213403

varbfl04	-0.339642	0.239818	-1.416	0.156702
varbhdct02	1.996726	0.323007	6.182	6.34e-10
varbhdct03	2.014335	0.287024	7.018	2.25e-12
varbhdct04	2.525820	0.277131	9.114	< 2e-16
varbld02	-0.971302	0.312215	-3.111	0.001865
varbld03	0.775863	0.393076	1.974	0.048402
varbld04	3.897397	0.330949	11.776	< 2e-16
nsloc	0.013538	0.001727	7.838	4.59e-15
ewloc	0.005990	0.001724	3.474	0.000513
siteEriley	0.332627	0.152129	2.186	0.028780
siteLf	0.318859	0.162391	1.964	0.049584
siteNessman	0.211191	0.187665	1.125	0.260435
siteNWLF	0.017505	0.142818	0.123	0.902449
siteSPP	0.168390	0.156462	1.076	0.281822
siteStevens	-0.083259	0.150749	-0.552	0.580741
siteEriley:hdct	-0.717275	0.259529	-2.764	0.005714
siteLf:hdct	-0.678378	0.278899	-2.432	0.015001
siteNessman:hdct	-0.673876	0.354761	-1.900	0.057496
siteNWLF:hdct	-0.127151	0.241487	-0.527	0.598518
siteSPP:hdct	-0.238292	0.258664	-0.921	0.356924
siteStevens:hdct	0.027072	0.256538	0.106	0.915956

Original predictor variables dropped (aliased)  
hdct

**Comment** The dropped (aliased) means just what it says. The R formula mini-language does not deal correctly with pseudo-covariates like this and thinks it should put (a dummy variable for) `hdct` in the model, but that is aliased with the sum of (the dummy variables for) `varbhdct02`, `varbhdct03`, and `varbhdct04`, so the `aster` function drops it, but not silently (so the user is not surprised).

It turns out this is not the model we wanted to fit. We didn't want site main effects, `siteEriley` and so forth, *in addition to* the site interaction effects `siteEriley:hdct` and so forth. We only wanted `site` to have effects at the `hdct` level. Here's how we do that

```
> aout4 <- aster(resp ~ varb + nsloc + ewloc + site *
+   hdct - site, pred, fam, varb, id, root, data = redata)
> summary(aout4)
```

Call:

```
aster.formula(formula = resp ~ varb + nsloc + ewloc + site *
  hdct - site, pred = pred, fam = fam, varvar = varb, idvar = id,
  root = root, data = redata)
```

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-1.463638	0.178183	-8.214	< 2e-16
varbfl03	-0.328488	0.265142	-1.239	0.215377
varbfl04	-0.349519	0.240775	-1.452	0.146601
varbhdct02	1.808447	0.258014	7.009	2.40e-12
varbhdct03	1.825590	0.210824	8.659	< 2e-16
varbhdct04	2.338955	0.197099	11.867	< 2e-16
varbld02	-0.989146	0.311742	-3.173	0.001509
varbld03	0.776572	0.392815	1.977	0.048049
varbld04	3.918323	0.330729	11.848	< 2e-16
nsloc	0.013600	0.001729	7.867	3.64e-15
ewloc	0.006473	0.001725	3.753	0.000174
siteEriley:hdct	-0.173902	0.089753	-1.938	0.052676
siteLf:hdct	-0.157706	0.096580	-1.633	0.102490
siteNessman:hdct	-0.315681	0.139822	-2.258	0.023962
siteNWLF:hdct	-0.109268	0.083325	-1.311	0.189740
siteSPP:hdct	0.023541	0.086552	0.272	0.785630
siteStevens:hdct	-0.127403	0.089518	-1.423	0.154677

Original predictor variables dropped (aliased)

hdct

and here's the ANOVA (analysis of deviance, log likelihood ratio test) table for these models

```
> anova(aout2, aout4, aout3)
```

Analysis of Deviance Table

Model 1: resp ~ varb + nsloc + ewloc

Model 2: resp ~ varb + nsloc + ewloc + site \* hdct - site

Model 3: resp ~ varb + nsloc + ewloc + site \* hdct

	Model Df	Model Dev	Df	Deviance	P(> Chi )
1	11	2747.90			
2	17	2731.95	6	15.95	0.01
3	23	2707.91	6	24.04	0.0005129

**Comment** When I did this the first time, I made the mistake of trying to put model `aout1` between `aout2` and `aout4`, but that’s the mistake we were warned about above! The models `aout2` and `aout4` are not nested! (This is obvious when you see they have the same degrees of freedom, and even more so when you think about the dummy variables they contain.) The only warning I got was about using zero degrees of freedom in a chi-square, not a warning about non-nested models. Be careful! (This warning goes for all uses of `anova` in R. It’s not only a problem with `anova.aster`.)

**Comment** That’s all for modeling of unconditional aster models. Note that these are not the spatial effects that were judged the best fitting in the paper. See the tech report (<http://www.stat.umn.edu/geyer/aster/>) for details.

### 3 Prediction

Once you have an aster model, it is a natural question to ask what it means. The `anova` tests give some information about this (which models fit better and which fit worse), but there is a lot more to statistics than hypothesis tests.

The other standard thing to do with regression-like models is to make confidence intervals for parameters. For reasons that don’t make any sense in the context of aster models, the function that does this is a method of the `predict` generic function (the reason is that for linear models only, this function does both confidence intervals and so-called prediction intervals).

With aster models we have a larve variety of parameters to “predict”. Every aster model comes with five different parameterizations

$\beta$  the regression coefficient vector,

$\theta$  the conditional canonical parameter vector,

$\varphi$  the unconditional canonical parameter vector,

$\xi$  the conditional mean value parameter vector, and

$\tau$  the unconditional mean value parameter vector.

#### 3.1 Regression Coefficients

The package provides no special support for confidence intervals about regression coefficients because of the dictum

Regression coefficients are meaningless. Only probabilities and expectations are meaningful.

In further support of the meaninglessness of regression coefficients note that two models specified by different model matrices that have the same *column spaces* are essentially the same model. The MLE regression coefficients will be different, but the MLE of  $\theta$ ,  $\varphi$ ,  $\xi$ , and  $\tau$  are identical for both models, as are predicted probabilities of all events and predicted expectations of all random variables. Once you understand that, how can you *reify* regression coefficients?

### 3.2 Using the Summary

Nevertheless, now that we have had our tendentious rant, we do tell you how to make confidence intervals for betas. The summary function gives standard errors, so one way is

```
> conf.level <- 0.95
> crit <- qnorm((1 + conf.level)/2)

> fred <- summary(aout4)
> dimnames(fred$coef)

[[1]]
[1] "(Intercept)"      "varbfl03"          "varbfl04"
[4] "varbhdct02"        "varbhdct03"        "varbhdct04"
[7] "varbld02"          "varbld03"          "varbld04"
[10] "nsloc"             "ewloc"             "siteEriley:hdct"
[13] "siteLf:hdct"       "siteNessman:hdct"  "siteNWLf:hdct"
[16] "siteSPP:hdct"      "siteStevens:hdct"

[[2]]
[1] "Estimate"  "Std. Error" "z value"    "Pr(>|z|)"

> fred$coef["siteEriley:hdct", "Estimate"] + c(-1,
+      1) * crit * fred$coef["siteEriley:hdct", "Std. Error"]

[1] -0.349813543  0.002010091
```

This gives an asymptotic (large sample) 95% confidence interval for the unknown true regression coefficient for the dummy variable `siteEriley:hdct` (assuming this model is correct!)

### 3.3 Using Fisher Information

Those who know master’s level theoretical statistics, know the standard error here is based on inverse Fisher information, which is found in the output of **aster**. So another way to do the same interval is

```
> aout4$coef[12] + c(-1, 1) * crit * sqrt(solve(aout4$fish)[12,
+      12])

[1] -0.349813543  0.002010091
```

### 3.4 Using Fisher Information (Continued)

The reason for even mentioning Fisher information is that it is essential if you want to make any other intervals for betas other than the ones **summary.aster** helps with. For example, suppose you want an interval for  $\beta_{12} - \beta_{13}$ . How do you do that?

```
> inv.fish.info <- solve(aout4$fish)
> (aout4$coef[12] - aout4$coef[13]) + c(-1, 1) * crit *
+   sqrt(inv.fish.info[12, 12] + inv.fish.info[13,
+      13] - 2 * inv.fish.info[12, 13])

[1] -0.1726329  0.1402422
```

If that doesn’t make sense, you’ll have to review your master’s level theory notes. We can’t explain everything. But fortunately, if you understand the meaninglessness of regression coefficients, you’ll never want to do that anyway.

### 3.5 Canonical Parameters

Canonical parameters are only slightly less meaningless than regression coefficients. They still aren’t probabilities and expectations that have real world meaning. However, **predict.aster** does give support for “predicting” canonical parameters.

There are, however a huge number of canonical parameters, one for each individual and node of the graphical model (same goes for mean value parameters). There are two ways we simplify the situation (both are standard in doing regression “predictions”)

- predict only for one (or a few) hypothetical or real “new” individuals and

- predict a linear functional of the parameter.

For the former we “predict” using a new model matrix whose entries refer to the “new” individuals rather than the “old” ones we used to fit the data. For the latter we predict  $\mathbf{A}'\boldsymbol{\zeta}$  where  $\mathbf{A}$  is a fixed, known matrix and  $\boldsymbol{\zeta}$  is the parameter we want to estimate (any of  $\boldsymbol{\theta}$ ,  $\boldsymbol{\varphi}$ ,  $\boldsymbol{\xi}$ , or  $\boldsymbol{\tau}$ ).

### 3.5.1 New Data

We construct new data for “typical” individuals (having zero-zero geometry) in each site.

```
> newdata <- data.frame(site = levels(echinacea$site))
> for (v in vars) newdata[[v]] <- 1
> newdata$root <- 1
> newdata$ewloc <- 0
> newdata$nsloc <- 0
```

We are using bogus data  $x_{ij} = 1$  for all  $i$  and  $j$ . The predictions for  $\boldsymbol{\theta}$  and  $\boldsymbol{\varphi}$  do not depend on new data anyway. Predictions for  $\boldsymbol{\tau}$  depend only on the new `root` data but not on the other data variables.

Predictions for  $\boldsymbol{\xi}$  do depend only on all the new data, but for hypothetical individuals we have no data to give them! This is an odd aspect of aster models, that data  $x_{ij}$  plays the role of the response and also of a predictor when it appears as  $x_{ip(j)}$ . The prediction section of the paper explains why we usually want this hypothetical data to be all ones.

```
> renewdata <- reshape(newdata, varying = list(vars),
+   direction = "long", timevar = "varb", times = as.factor(vars),
+   v.names = "resp")
> hdct <- grep("hdct", as.character(renewdata$varb))
> hdct <- is.element(seq(along = renewdata$varb), hdct)
> renewdata <- data.frame(renewdata, hdct = as.integer(hdct))
> names(redata)
```

```
[1] "site" "ewloc" "nsloc" "varb" "resp" "id" "root"
[8] "hdct"
```

```
> names(renewdata)
```

```
[1] "site" "root" "ewloc" "nsloc" "varb" "resp" "id"
[8] "hdct"
```

### 3.5.2 Linear Functional Matrix

The functional of mean value parameters we want is *total head count*, since this has the biological interpretation of the component of fitness measured in this data set. A biologist (at least an evolutionary biologist) is interested in the “predecessor variables” of head count only insofar as they contribute to head count. Two sets of parameter values that “predict” the same expected total head count (over the three years the data were collected) have the same contribution to fitness. So that is the “prediction” (really functional of mean value parameters) we “predict.”

```
> nind <- nrow(newdata)
> nnode <- length(vars)
> amat <- array(0, c(nind, nnode, nind))
> for (i in 1:nind) amat[i, grep("hdct", vars), i] <- 1
```

This says that the  $i$ -th component of the predicted linear functional is the sum of the variables having "hdct" in their names for the  $i$ -th individual (in the new hypothetical data `newdata`). The linear functional is a simple sum because the elements of `amat` are all zero or one.

### 3.5.3 Prediction

So we are finally ready to make a “prediction”

```
> foo <- predict(aout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = amat, parm.type = "canon")
> bar <- cbind(foo$fit, foo$se.fit)
> dimnames(bar) <- list(as.character(newdata$site),
+   c("Estimate", "Std. Error"))
> print(bar)
```

	Estimate	Std. Error
AA	1.5820795	0.2478499
Eriley	1.0603744	0.1972253
Lf	1.1089604	0.2239097
Nessman	0.6350351	0.3800243
NWLF	1.2542756	0.1679685
SPP	1.6527033	0.1746258
Stevens	1.1998709	0.1945909



Since the default `model.type` is "unconditional", these are (linear functionals of) the unconditional canonical parameters  $\varphi$ .

And for our next trick (neither of these are motivated by a particular scientific question—we're just illustrating the use of `predict.aster`).

```
> foo <- predict(aout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = amat, parm.type = "canon", model.type = "cond")
> bar <- cbind(foo$fit, foo$se.fit)
> dimnames(bar) <- list(as.character(newdata$site),
+   c("Estimate", "Std. Error"))
> print(bar)
```

	Estimate	Std. Error
AA	1.5820795	0.2478499
Eriley	1.0603744	0.1972253
Lf	1.1089604	0.2239097
Nessman	0.6350351	0.3800243
NWLF	1.2542756	0.1679685
SPP	1.6527033	0.1746258
Stevens	1.1998709	0.1945909

These are (linear functionals of) the conditional canonical parameters  $\theta$ .

Woof! When I saw this the first time, I spent over an hour trying to track down the bug in `predict.aster` that gives the same predictions for two different types of parameters. But it's not a bug. The canonical parameters for "leaf" nodes (no successors) *are* the same!

Let's try the "ld" level (mortality)

```
> bmat <- array(0, c(nind, nnode, nind))
> for (i in 1:nind) bmat[i, grep("ld", vars), i] <- 1

> foo <- predict(aout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = bmat, parm.type = "canon")
> bar <- cbind(foo$fit, foo$se.fit)
> dimnames(bar) <- list(as.character(newdata$site),
+   c("Estimate", "Std. Error"))
> print(bar)
```

	Estimate	Std. Error
AA	-0.6851641	0.1271524

Eriley	-0.6851641	0.1271524
Lf	-0.6851641	0.1271524
Nessman	-0.6851641	0.1271524
NWLF	-0.6851641	0.1271524
SPP	-0.6851641	0.1271524
Stevens	-0.6851641	0.1271524

```
> foo <- predict(aout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = bmat, parm.type = "canon", model.type = "cond")
> bar <- cbind(foo$fit, foo$se.fit)
> dimnames(bar) <- list(as.character(newdata$site),
+   c("Estimate", "Std. Error"))
> print(bar)
```

	Estimate	Std. Error
AA	7.944257	0.6177680
Eriley	6.928158	0.4348137
Lf	7.009798	0.4758742
Nessman	6.307471	0.5759345
NWLF	7.268865	0.4173700
SPP	8.108078	0.4831169
Stevens	7.169185	0.4481993

Now quite different! And we have another puzzle. Why, according to aster model theory is it the right thing that all of the  $\xi_{ij}$  are the same where  $j$  is for an "ld" node? Just look at the model, we don't have an interaction of ld and site.

```
> foo <- predict(aout3, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = bmat, parm.type = "canon")
> bar <- cbind(foo$fit, foo$se.fit)
> dimnames(bar) <- list(as.character(newdata$site),
+   c("Estimate", "Std. Error"))
> print(bar)
```

	Estimate	Std. Error
AA	-1.04898992	0.4036746
Eriley	-0.05110772	0.2496746
Lf	-0.09241159	0.3025186

Nessman	-0.41541594	0.4080958
NWLF	-0.99647496	0.1949520
SPP	-0.54382117	0.2825132
Stevens	-1.29876764	0.2422731

If instead we use the model `aout3`, which does have such an interaction (the interaction is with `non-hdct`, but that includes `ld`), then the  $\xi_{ij}$  are different.

What this all proves other than that aster models are complicated, I don't know. The point is just to give some examples. We don't think scientists should want to "predict" canonical parameters much (except perhaps just to see what's going on under the hood of some model).

### 3.6 Mean Value Parameters

To repeat our mantra

Only probabilities and expectations are meaningful.

The parameters that `predict.aster` can predict and that are meaningful (according to our mantra) are *mean value parameters*. As with everything else, there are two kinds, conditional and unconditional ( $\xi$  and  $\tau$ , respectively).

Let's try that.

```
> pout3 <- predict(aout3, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = amat)
> pout4 <- predict(aout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = amat)
```

Figure 1 is produced by the following code

```
> sitenames <- as.character(newdata$site)
> fit3 <- pout3$fit
> fit4 <- pout4$fit
> i <- seq(along = sitenames)
> foo <- 0.1
> y4top <- fit4 + crit * pout4$se.fit
> y4bot <- fit4 - crit * pout4$se.fit
> y3top <- fit3 + crit * pout3$se.fit
> y3bot <- fit3 - crit * pout3$se.fit
```

```

> plot(c(i - 1.5 * foo, i - 1.5 * foo, i + 1.5 * foo,
+       i + 1.5 * foo), c(y4top, y4bot, y3top, y3bot),
+       type = "n", axes = FALSE, xlab = "", ylab = "")
> segments(i - 1.5 * foo, y4bot, i - 1.5 * foo, y4top)
> segments(i - 2.5 * foo, y4bot, i - 0.5 * foo, y4bot)
> segments(i - 2.5 * foo, y4top, i - 0.5 * foo, y4top)
> segments(i - 2.5 * foo, fit4, i - 0.5 * foo, fit4)
> segments(i + 1.5 * foo, y3bot, i + 1.5 * foo, y3top,
+       lty = 2)
> segments(i + 2.5 * foo, y3bot, i + 0.5 * foo, y3bot)
> segments(i + 2.5 * foo, y3top, i + 0.5 * foo, y3top)
> segments(i + 2.5 * foo, fit3, i + 0.5 * foo, fit3)
> axis(side = 2)
> title(ylab = "unconditional mean value parameter")
> axis(side = 1, at = i, labels = sitenames)
> title(xlab = "site")

```

and appears on p. 21.

Figure 1 looks pretty much like the plot in the paper. It’s a little different because the spatial part of the model (involving `ewloc` and `nsloc` is simpler).

These confidence intervals have real-world meaning. The parameters predicted are “components of fitness” (expected flower head count over the course of the experiment) for “typical” individuals (“typical” spatial location smack dab in the middle because we centered the spatial coordinates to have median zero) at each of the sites. (BTW I have no idea why `axis` leaves off one of the site labels when there’s plenty of room. To get this plot right for the paper I just edited the PostScript file and put in the missing label by hand. If you ask me, it’s a bug. But the `axis` maintainer would probably say it’s a feature.)

As we have seen, you can “predict” any kind of parameter ( $\beta$ ,  $\theta$ ,  $\varphi$ ,  $\xi$ , or  $\tau$ ) for any model. All of the examples so far have been unconditional aster models (FEF). But we could have done everything above if we had originally fit conditional aster models (CEF).

## 4 Conditional Aster Models

We could now repeat everything above *mutatis mutandis*. The only thing that would change is an argument `type = "conditional"` to any call to the `aster` function. Then everything else works exactly the same (of course the actual numerical results are different, but the other function calls to

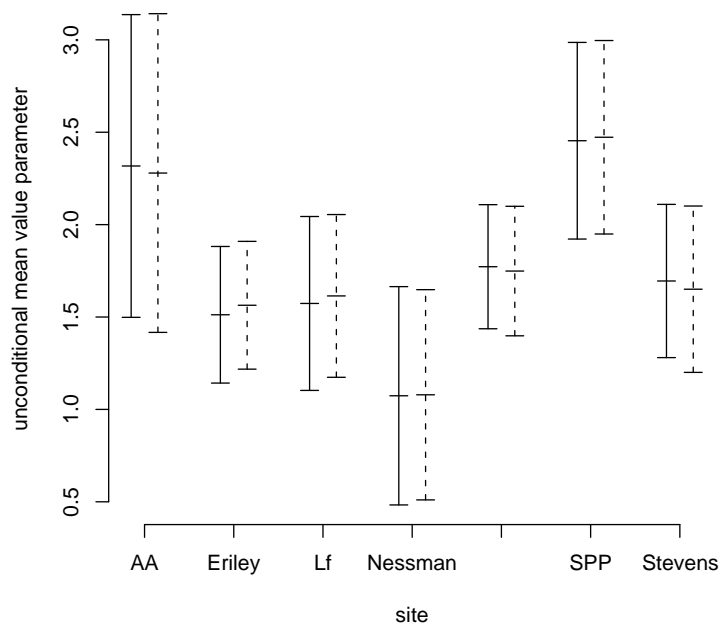


Figure 1: 95% confidence intervals for unconditional mean value parameter for fitness (sum of head count for all years) at each site for a “typical” individual having position zero-zero and having the parameterization of Model 4 (solid bar) or Model 3 (dashed bar). Tick marks in the middle of the bars are the center (the MLE).

summary.aster, anova.aster, or predict.aster are meaningful without change).

Let's look at one example.

```
> cout4 <- aster(resp ~ varb + nsloc + ewloc + site *
+   hdct - site, pred, fam, varb, id, root, data = redata,
+   type = "cond")
> pcout4 <- predict(cout4, varvar = varb, idvar = id,
+   root = root, newdata = renewdata, se.fit = TRUE,
+   amat = amat)
```

Note that these are exactly the same as the commands that made pout4 except for the extra argument `type = "cond"` in the `aster` function call. Thus we have fit a conditional aster model (CEF) but predicted exactly the same  $\mathbf{A}'\boldsymbol{\tau}$  as in pout4.

Figure 2 compares these two “predictions” and is produced by the following code

```
> sitenames <- as.character(newdata$site)
> fit3 <- pcout4$fit
> fit4 <- pout4$fit
> i <- seq(along = sitenames)
> foo <- 0.1
> y4top <- fit4 + crit * pout4$se.fit
> y4bot <- fit4 - crit * pout4$se.fit
> y3top <- fit3 + crit * pcout4$se.fit
> y3bot <- fit3 - crit * pcout4$se.fit
> plot(c(i - 1.5 * foo, i - 1.5 * foo, i + 1.5 * foo,
+   i + 1.5 * foo), c(y4top, y4bot, y3top, y3bot),
+   type = "n", axes = FALSE, xlab = "", ylab = "")
> segments(i - 1.5 * foo, y4bot, i - 1.5 * foo, y4top)
> segments(i - 2.5 * foo, y4bot, i - 0.5 * foo, y4bot)
> segments(i - 2.5 * foo, y4top, i - 0.5 * foo, y4top)
> segments(i - 2.5 * foo, fit4, i - 0.5 * foo, fit4)
> segments(i + 1.5 * foo, y3bot, i + 1.5 * foo, y3top,
+   lty = 2)
> segments(i + 2.5 * foo, y3bot, i + 0.5 * foo, y3bot)
> segments(i + 2.5 * foo, y3top, i + 0.5 * foo, y3top)
> segments(i + 2.5 * foo, fit3, i + 0.5 * foo, fit3)
> axis(side = 2)
> title(ylab = "unconditional mean value parameter")
```

```
> axis(side = 1, at = i, labels = sitenames)
> title(xlab = "site")
```

and appears on p. 24.

Now note that the two types of intervals (solid and dashed) are wildly different. Of course, they *should* be wildly different because the two types of models, one with  $\varphi = \mathbf{M}\beta$  and the other with  $\theta = \mathbf{M}\beta$ , are radically different. There is no reason for the two types of predictions (of exactly the same thing) based on two radically different models should be similar. And they aren't. So we are only seeing what we should expect to see, and this doesn't prove anything about anything (except for the trivial fact that FEF and CEF aster models are different).

**Comment** We haven't really done justice to conditional models. Since this is a tutorial, we don't have to. As we said (twice), everything is the same except for `type = "cond"` in the appropriate place.

And this is not the place to explain why one would want to use a conditional or unconditional model. And, to be honest, we don't know. We know, and explain in the paper, what each one does and why

Conditional aster models are simple algebraically, but complicated statistically.

Unconditional aster models are complicated algebraically, but simple statistically.

But we have to admit that these arguments from theoretical statistics may cut no ice with scientists, even if understood. It all depends on what particular scientific questions one is trying to answer. Thus we have written the **aster** package to be completely even-handed (except for defaults) with respect to conditional and unconditional (models or parameters). Whatever can be done with one kind can be done with the other. So use whatever you think right.

## 5 Simulation

One function we haven't covered is **raster** which simulates aster models. Let's check the coverage of some of our so-called 95% confidence intervals.

We start with another use of **predict**. The **raster** function wants  $\theta$  or, to be more precise, here we use  $\hat{\theta}$ .

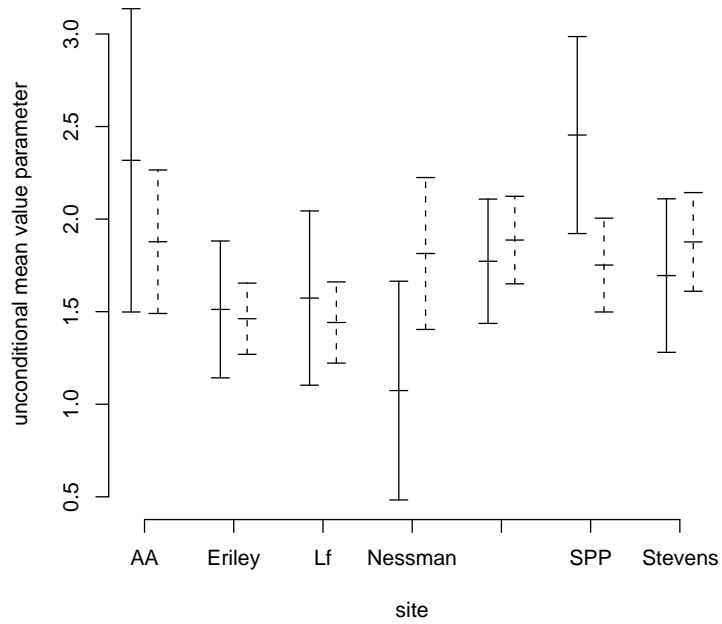


Figure 2: 95% confidence intervals for unconditional mean value parameter for fitness (sum of head count for all years) at each site for a “typical” individual having position zero-zero and having the parameterization of Model 4, either an unconditional model (solid bar) or conditional model (dashed bar). Tick marks in the middle of the bars are the center (the MLE).



```

> theta.hat <- predict(aout4, model.type = "cond",
+   parm.type = "canon")
> theta.hat <- matrix(theta.hat, nrow = nrow(aout4$x),
+   ncol = ncol(aout4$x))
> fit.hat <- pout4$fit
> beta.hat <- aout4$coefficients

```

We also need root data, and it will be simpler if we actually don't use the forms of the `aster` and `predict.aster` functions that take formulas (because then we don't have to cram the simulated data in a data frame and we avoid a lot of repetitive parsing of the same formulas)

```

> root <- aout4$root
> modmat <- aout4$modmat
> modmat.pred <- pout4$modmat
> x.pred <- matrix(1, nrow = dim(modmat.pred)[1], ncol = dim(modmat.pred)[2])
> root.pred <- x.pred

```

Now we're ready for a simulation

```

> set.seed(42)
> nboot <- 100
> cover <- matrix(0, nboot, length(fit.hat))
> for (iboot in 1:nboot) {
+   xstar <- raster(theta.hat, pred, fam, root)
+   aout4star <- aster(xstar, root, pred, fam, modmat,
+     beta.hat, check.analyticals = FALSE)
+   pout4star <- predict(aout4star, x.pred, root.pred,
+     modmat.pred, amat, se.fit = TRUE)
+   upper <- pout4star$fit + crit * pout4star$se.fit
+   lower <- pout4star$fit - crit * pout4star$se.fit
+   cover[iboot, ] <- as.numeric(lower <= fit.hat &
+     fit.hat <= upper)
+ }
> pboot <- apply(cover, 2, mean)
> pboot.se <- sqrt(pboot * (1 - pboot)/nboot)
> cbind(pboot, pboot.se)

```

```

      pboot  pboot.se
[1,]  0.91 0.02861818
[2,]  0.98 0.01400000
[3,]  0.94 0.02374868

```

```
[4,] 0.91 0.02861818
[5,] 0.94 0.02374868
[6,] 0.96 0.01959592
[7,] 0.94 0.02374868
```

Not bad for the small `nboot`. We won't try a serious simulation because it would make this tutorial run too long.

**Comment** The `check.analyticals = FALSE` argument is passed to `nlm` which actually does the optimization. (The code we wrote only calculates the log likelihood and its derivatives.) Other optimization options (calling `optim` are available), but we haven't done extensive testing to see which is better (HmMMM. Well on this job, using `method = "L-BFGS-B"` takes about four times longer than the default and `method = "CG"` takes about eight times longer. So whatever problems `optim` is good for, it doesn't appear to be strictly convex objective functions like aster models have.) The starting parameter value `beta.hat` is supposed to speed things up, giving the optimization a good starting point (the simulation truth), but `nlm` still takes 150 iterations or so (not shown).