

Management frequency and extinction risk

GMSE: an R package for generalised management strategy evaluation (Supporting Information 6)

A. Bradley Duthie^{1,3}, Jeremy J. Cusack¹, Isabel L. Jones¹, Jeroen Minderman¹, Erlend B. Nilsen², Rocío A. Pozo¹, O. Sarobidy Rakotonarivo¹, Bram Van Moorter², and Nils Bunnefeld¹

[1] Biological and Environmental Sciences, University of Stirling, Stirling, UK [2] Norwegian Institute for Nature Research, Trondheim, Norway [3] alexander.duthie@stir.ac.uk

The individual-based approach of default GMSE sub-models

The default sub-models of GMSE (`resource`, `observation`, `manager`, `user`) are individual-based (also called ‘agent-based’), meaning that they model discrete individuals (resources or agents), which in GMSE are represented by individual table rows (as in `RESOURCES`, `AGENTS`, and `OBSERVATION`) or layers of three-dimensional arrays (as in `COST` and `ACTION`). Individual-based models (IBMs) have been a useful approach in ecology for decades (Uchmański and Grimm, 1996; Grimm, 1999), providing both a pragmatic tool for the mechanistic modelling of complex populations and a powerful technique for theoretical investigation. A key advantage of the individual-based modelling approach is the discrete nature of individuals, which allows for detailed trait variation and complex interactions among individuals. In GMSE, some of the most important traits for resources include types, ages, demographic parameter values, locations, etc., and for agents (manager and users), traits include different types, utilities, budgets, etc. The traits that resources and managers have can potentially affect their interactions, and default GMSE sub-models take advantage of this by simulating interactions explicitly on a landscape (see SI7 for an introduction to GMSE default data structures).

Replicate simulations as a tool for model inference

Mechanistically modelling complex interactions among discrete individuals typically causes some degree of stochasticity in IBMs (in the code, this is caused by the sampling of random values, which determine probabilistically whether or not events such as birth or death occur for individuals), reflecting the uncertainty that is inherent to complex systems. We can see a simple example of this by calling `gmse_apply` under the same default conditions twice.

```
rand_eg_1 <- gmse_apply();  
print(rand_eg_1);
```

```
## $resource_results  
## [1] 1118  
##  
## $observation_results  
## [1] 1451.247  
##  
## $manager_results  
##           resource_type scaring culling castration feeding help_offspring  
## policy_1             1      NA      45      NA      NA      NA  
##  
## $user_results  
##           resource_type scaring culling castration feeding help_offspring
```

```

41 ## Manager      1      NA      0      NA      NA      NA
42 ## user_1       1      NA     22      NA      NA      NA
43 ## user_2       1      NA     22      NA      NA      NA
44 ## user_3       1      NA     22      NA      NA      NA
45 ## user_4       1      NA     22      NA      NA      NA
46 ##             tend_crops kill_crops
47 ## Manager      NA      NA
48 ## user_1       NA      NA
49 ## user_2       NA      NA
50 ## user_3       NA      NA
51 ## user_4       NA      NA

```

Although a second call of `gmse_apply` has identical initial conditions, because resource demographics (e.g., birth and death) and agent decision making (e.g., policy generation and user actions) is not deterministic, a slightly different result is obtained below.

```

rand_eg_2 <- gmse_apply();
print(rand_eg_2);

```

```

55 ## $resource_results
56 ## [1] 1090
57 ##
58 ## $observation_results
59 ## [1] 839.0023
60 ##
61 ## $manager_results
62 ##             resource_type scaring culling castration feeding help_offspring
63 ## policy_1      1      NA     66      NA      NA      NA
64 ##
65 ## $user_results
66 ##             resource_type scaring culling castration feeding help_offspring
67 ## Manager      1      NA      0      NA      NA      NA
68 ## user_1       1      NA     15      NA      NA      NA
69 ## user_2       1      NA     15      NA      NA      NA
70 ## user_3       1      NA     15      NA      NA      NA
71 ## user_4       1      NA     15      NA      NA      NA
72 ##             tend_crops kill_crops
73 ## Manager      NA      NA
74 ## user_1       NA      NA
75 ## user_2       NA      NA
76 ## user_3       NA      NA
77 ## user_4       NA      NA

```

To make meaningful model inferences, it is often necessary to replicate simulations under the same initial conditions to understand the range of predicted outcomes for a particular set of parameter values. This can be computationally intense, but it can also lead to a more robust understanding of the range of dynamics that might be expected within a system. Additionally, when parameter values are unknown but believed to be important, replicate simulations can be applied across a range of values to understand how a particular parameter might affect system dynamics. Below, we show how to use the `gmse_replicates` function to simulate a simple example of a managed population that is hunted by users. This function calls `gmse` multiple times and aggregates the results from replicate simulations into a single table.

For a single simulation, the `gmse_table` function prints out key information from a `gmse` simulation result. The example provided in the [GMSE documentation](#) is below.

```
gmse_sim <- gmse(time_max = 10, plotting = FALSE);
```

```
## [1] "Initialising simulations ... "
```

```
sim_table <- gmse_table(gmse_sim = gmse_sim);
print(sim_table)
```

```
##      time_step resources  estimate cost_culling cost_unused act_culling
## [1,]         1      1106 1088.4354          57          53          68
## [2,]         2      1147 1179.1383          20          90         200
## [3,]         3      1051 1043.0839          83          27          48
## [4,]         4      1157  997.7324         110           0          36
## [5,]         5      1302 1111.1111          33          77         120
## [6,]         6      1572 1473.9229          10         100         400
## [7,]         7      1397 1451.2472          10         100         400
## [8,]         8      1237 1383.2200          10         100         400
## [9,]         9       1006 1111.1111          32          78         124
## [10,]        10       1062  634.9206         110           0          36
##      act_unused harvested
## [1,]          6         68
## [2,]          0        200
## [3,]          0         48
## [4,]          2         36
## [5,]          2        120
## [6,]          0        400
## [7,]          0        400
## [8,]          0        400
## [9,]          0        124
## [10,]         3         36
```

The above table can be saved as a CSV file using the `write.csv` function.

```
write.csv(x= sim_table, file = "file_path/gmse_table_name.csv");
```

Instead of recording all time steps in the simulation, we can instead record only the last time step in `gmse_table` using the `all_time` argument.

```
sim_table_last <- gmse_table(gmse_sim = gmse_sim, all_time = FALSE);
print(sim_table_last)
```

```
##      time_step  resources  estimate cost_culling cost_unused
##      10.0000   1062.0000   634.9206    110.0000     0.0000
##  act_culling  act_unused  harvested
##      36.0000     3.0000    36.0000
```

The `gmse_replicates` function replicates multiple simulations `replicates` times under the same initial conditions, then returns a table showing the values of all simulations. This can be useful, for example, for testing how frequently a population is expected to go to extinction or carrying capacity under a given set of parameter values. First, we demonstrate the `gmse_replicates` function for simulations of up to 20 time steps. The `gmse_replicates` function accepts all arguments used in `gmse`, and also all arguments of `gmse_table` (`all_time` and `hide_unused_options`) to summarise multiple `gmse` results. Here we use default `gmse` values in replicate simulations, except `plotting`, which we set to `FALSE` to avoid plotting each simulation result. We run 10 replicates below.

```
gmse_reps1 <- gmse_replicates(replicates = 10, time_max = 20, plotting = FALSE);
print(gmse_reps1);
```

```
##      time_step resources  estimate cost_culling cost_unused act_culling
```

```

127 ## [1,]      20      1436 1473.9229      10      100      400
128 ## [2,]      20      1273 1269.8413      13       97      304
129 ## [3,]      20      1243 1269.8413      13       97      304
130 ## [4,]      20      1191 1088.4354      41       69       96
131 ## [5,]      20       849 1020.4082     109        0       36
132 ## [6,]      20      1616 1904.7619      10      100      400
133 ## [7,]      20      1039 997.7324     110        0       36
134 ## [8,]      20       968 907.0295     110        0       36
135 ## [9,]      20      1403 1587.3016      10      100      400
136 ## [10,]     20       983 884.3537     110        0       36
137 ##      act_unused harvested
138 ## [1,]         0       400
139 ## [2,]         2       304
140 ## [3,]         3       304
141 ## [4,]         2        96
142 ## [5,]         1        36
143 ## [6,]         0       400
144 ## [7,]         1        36
145 ## [8,]         1        36
146 ## [9,]         0       400
147 ## [10,]        2        36

```

148 Note from the results above that resources in all simulations persisted for 20 time steps, which means that
149 extinction never occurred. We can also see that the population in all simulations never terminated at a density
150 near the default carrying capacity of `res_death_K = 2000`, and was instead consistently near the target
151 population size of `manage_target = 1000`. If we wish to define management success as having a population
152 density near target levels after 20 time steps (perhaps interpreted as 20 years), then we might assess this
153 population as successfully managed under the conditions of the simulation. We can then see what happens if
154 managers only respond to changes in the social-ecological system with a change in policy once every two
155 years, perhaps as a consequence of reduced funding for management or increasing demands for management
156 attention elsewhere. This can be done by changing the default `manage_freq = 1` to `manage_freq = 2`.

```

gmse_reps2 <- gmse_replicates(replicates = 10, time_max = 20, plotting = FALSE,
                             manage_freq = 2);
print(gmse_reps2);

```

```

157 ##      time_step resources estimate cost_culling cost_unused act_culling
158 ## [1,]         20      1100 1065.7596        55        55        72
159 ## [2,]         20       625 476.1905        110         0        36
160 ## [3,]         20       864 952.3810        110         0        36
161 ## [4,]         20      1034 929.7052        108         2        36
162 ## [5,]         20      1370 1519.2744         10      100      400
163 ## [6,]         20      1255 1451.2472         10      100      400
164 ## [7,]         20      1036 1315.1927         12       98      332
165 ## [8,]         20       932 997.7324        110         0        36
166 ## [9,]         20      1439 997.7324        110         0        36
167 ## [10,]        20      1118 1043.0839         84        26        44
168 ##      act_unused harvested
169 ## [1,]         2         72
170 ## [2,]         2         36
171 ## [3,]         2         36
172 ## [4,]         5         36
173 ## [5,]         0       400
174 ## [6,]         0       400
175 ## [7,]         0      332

```

```

176 ## [8,]          1          36
177 ## [9,]          2          36
178 ## [10,]         7          44

```

179 Note that while extinction still does not occur in these simulations, when populations are managed less
 180 frequently, they tend to be less close to the target size of 1000 after 20 generations. The median population
 181 size of `gmse_reps1` (management in every time step) was 1217, with a maximum of 1616 and minimum of
 182 849. The median population size of the newly simulated `gmse_reps2` (management every two time steps)
 183 is 1068, with a maximum of 1439 and minimum of 625. We can now see what happens when management
 184 occurs only once in every three time steps.

```

gmse_reps3 <- gmse_replicates(replicates = 10, time_max = 20, plotting = FALSE,
                             manage_freq = 3);
print(gmse_reps3);

```

```

185 ##      time_step resources  estimate cost_culling cost_unused act_culling
186 ## [1,]         20        800  702.9478         110          0          36
187 ## [2,]         20       1309  839.0023         110          0          36
188 ## [3,]         20        991  884.3537         109          1          36
189 ## [4,]         20        669  498.8662         110          0          36
190 ## [5,]         20       1074 1179.1383          20         90         200
191 ## [6,]         20       1221 1315.1927          12        98         332
192 ## [7,]         20       1061  748.2993         110          0          36
193 ## [8,]         20       1183  975.0567         110          0          36
194 ## [9,]         20       1197  725.6236         108          2          36
195 ## [10,]        20        520 1360.5442          10        100         400
196 ##      act_unused harvested
197 ## [1,]          1          36
198 ## [2,]          2          36
199 ## [3,]          0          36
200 ## [4,]          0          36
201 ## [5,]          0         200
202 ## [6,]          0         332
203 ## [7,]          2          36
204 ## [8,]          1          36
205 ## [9,]          2          36
206 ## [10,]         0         400

```

207 Given a management frequency of once every three time steps, the median population size of `gmse_reps3`
 208 (management in every time step) is 1067.5, with a maximum of 1309 and minimum of 520. The number of
 209 extinctions observed in these replicate populations was 0. Below we change the management frequency to
 210 once every four time steps.

```

gmse_reps4 <- gmse_replicates(replicates = 10, time_max = 20, plotting = FALSE,
                             manage_freq = 4);
print(gmse_reps4);

```

```

211 ##      time_step resources  estimate cost_culling cost_unused act_culling
212 ## [1,]         20       2027 1904.76190          10        100         400
213 ## [2,]         20        203  204.08163         110          0          36
214 ## [3,]         20       1904 1791.38322          10        100         400
215 ## [4,]         13          3   22.67574         110          0          36
216 ## [5,]         11          0   68.02721         110          0          36
217 ## [6,]         15          0 1405.89569          10        100         400
218 ## [7,]         20       1948 1950.11338          10        100         400
219 ## [8,]         20        834  975.05669         110          0          36

```

```

220 ## [9,]          20          29  0.00000          110          0          36
221 ## [10,]         20        1833 1473.92290          10        100        400
222 ##      act_unused harvested
223 ## [1,]           0         400
224 ## [2,]           0          36
225 ## [3,]           0         400
226 ## [4,]           2           3
227 ## [5,]           2           0
228 ## [6,]           0           0
229 ## [7,]           0         400
230 ## [8,]           1          36
231 ## [9,]           1          29
232 ## [10,]          0         400

```

233 Now note from the first column of `gmse_reps4` above that 3 populations did not persist to the 20th time
 234 step; i.e., 3 populations went to extinction (note that GMSE has a minimum resource population size of 5).
 235 This has occurred because managers cannot respond quickly enough to changes in the population density, and
 236 therefore cannot increase the cost of culling to maintain target resource levels if population size starts to
 237 decrease. We can see the extinction risk increase even further if management only occurs once every 5 time
 238 steps.

```

gmse_reps5 <- gmse_replicates(replicates = 10, time_max = 20, plotting = FALSE,
                             manage_freq = 5);
print(gmse_reps5);

```

```

239 ##      time_step resources estimate cost_culling cost_unused act_culling
240 ## [1,]          5           0           0          110           0          36
241 ## [2,]          5           0           0          110           0          36
242 ## [3,]          5           0           0          110           0          36
243 ## [4,]          5           0           0          110           0          36
244 ## [5,]          5           0           0          110           0          36
245 ## [6,]          5           0           0          110           0          36
246 ## [7,]          5           0           0          110           0          36
247 ## [8,]          5           0           0          110           0          36
248 ## [9,]          5           0           0          110           0          36
249 ## [10,]         5           0           0          109           1          36
250 ##      act_unused harvested
251 ## [1,]           2           0
252 ## [2,]           1           0
253 ## [3,]           1           0
254 ## [4,]           2           0
255 ## [5,]           1           0
256 ## [6,]           1           0
257 ## [7,]           0           0
258 ## [8,]           0           0
259 ## [9,]           2           0
260 ## [10,]          1           0

```

261 When a manager can only make policy decisions once every five time steps, extinction occurs in 10 out of 10
 262 simulated populations before year 20. If we wanted to summarise these results, we could plot how extinction
 263 risk changes with increasing `manage_freq`.

```

ext_risk1 <- sum(gmse_reps1[,2] < 20);
ext_risk2 <- sum(gmse_reps2[,2] < 20);
ext_risk3 <- sum(gmse_reps3[,2] < 20);
ext_risk4 <- sum(gmse_reps4[,2] < 20);

```

```

ext_risk5 <- sum(gmse_reps5[,2] < 20);
y_var      <- c(ext_risk1, ext_risk2, ext_risk3, ext_risk4, ext_risk5);
x_var      <- 1:5;
plot(x = x_var, y = y_var, type = "b", pch = 20, lwd = 2, cex = 1.5,
     xlab = "Management every N time steps (manage_freq)",
     ylab = "Freq. of population extinction", cex.lab = 1.25)

```

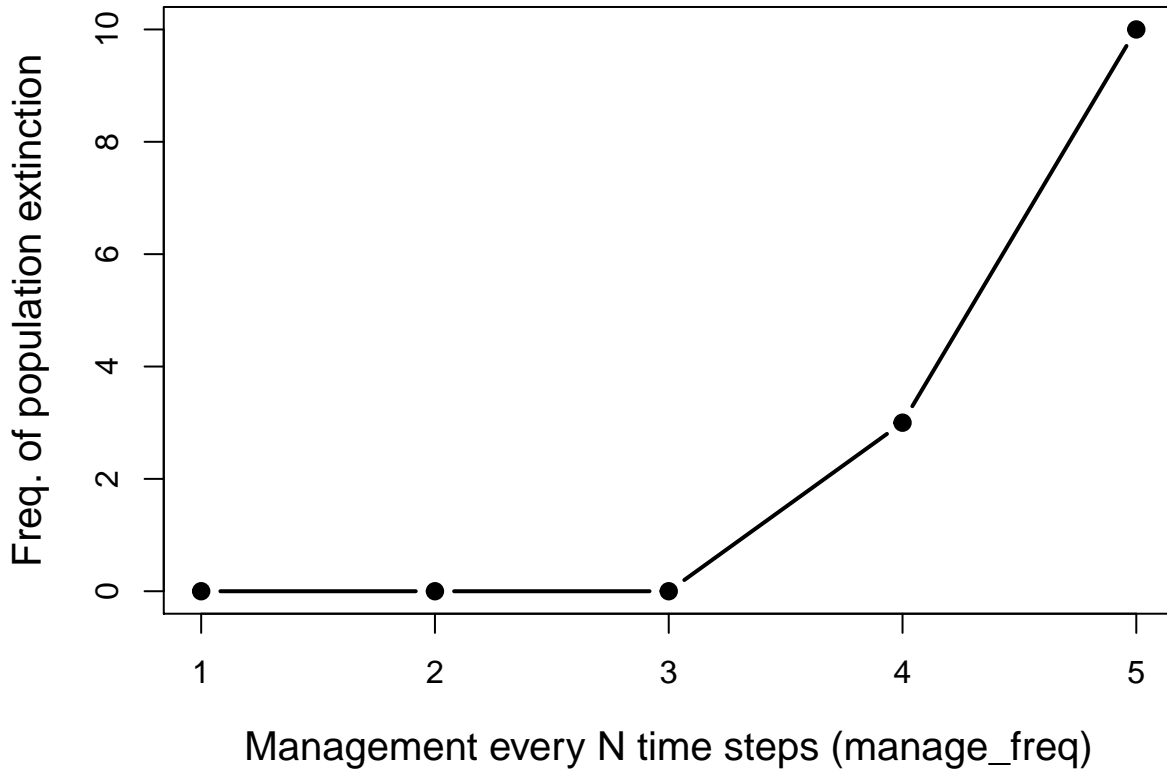


Figure 1: Extinction risk given an increasing number of time steps between updating policy decisions for culling costs in a simulated population. Higher values on the x-axis correspond to more time passing before a new policy is set. For each point, a total of 10 replicate simulations were run.

The above plot and the simulations from which it was derived illustrates a greatly simplified example of how GMSE might be used to assess the risk of extinction in a managed population. A comprehensive analysis would need more than 10 replicate simulations to accurately infer extinction risk, and would require careful parameterisation of all sub-models and a sensitivity analysis where such parameters are unknown. A benefit of this approach is that it allows for the simulation of multiple different scenarios under conditions of uncertainty and stochasticity, modelling the range of outcomes that might occur within and among scenarios and facilitating the development of social-ecological theory. Future expansion on the complexity of individual-based default sub-models of GMSE will further increase the realism of targeted case studies.

References

- Grimm, V. (1999). Ten years of individual-based modelling in ecology: what have we learned and what could we learn in the future? *Ecological Modelling*, 115(2-3):129–148.
- Uchmański, J. and Grimm, V. (1996). Individual-based modelling in ecology: what makes the difference? *Trends in Ecology & Evolution*, 11(10):437–441.